

Math 10A

Quiz 4; Tuesday, 7/2/2018

Time: 3 PM

Instructor: Roy Zhao

Name: _____

Circle True or False. (1 point for correct answer, 0 if incorrect)

1. True **FALSE** If we take $\lim_{x \rightarrow \infty} f(x)^{g(x)}$ and get 1^∞ , then the limit is 1.

Solution: We need to change it to use L'Hopital's Rule.

2. True **FALSE** If we take $\lim_{x \rightarrow \infty} f(x)^{g(x)}$ and get 0^∞ , then we need to use L'Hopital's Rule.

Solution: The limit is then 0.

Show your work and justify your answers. Please circle or box your final answer.

3. (10 points) (a) (3 points) Find $\lim_{x \rightarrow 0} \frac{x \tan x}{\sin 3x}$.

Solution: Plugging in $x = 0$ gives $0/0$ so using Lhopitals gives

$$\lim_{x \rightarrow 0} \frac{x \tan x}{\sin 3x} = \lim_{x \rightarrow 0} \frac{x \sec^2(x) + \tan x}{3 \cos(3x)} = \frac{0}{3} = 0.$$

- (b) (7 points) Sand is being dumped in a conical pile whose width and height always remain the same. If the sand is being dumped in at a rate of $5\pi \text{ cm}^3/\text{min}$, how fast is the height of the sand changing when the pile is 10 cm tall?

Solution: Let the height of the pile be h . Then the radius of the pile is $r = \frac{h}{2}$ and the volume of the pile is $V = \frac{\pi r^2 h}{3} = \frac{\pi h^3}{12}$. Taking the derivative gives $V' = \frac{\pi}{4} h^2 h'$. Now we plug in 5π for V' and 10 for h to get $h' = \frac{20\pi}{100\pi} = \frac{1}{5}$ cm/min.